

# Fully Automated Shape Analysis Based on Forest Automata<sup>†</sup>

Lukáš Holík   **Ondřej Lengál**   Adam Rogalewicz  
Jiří Šimáček   Tomáš Vojnar

Brno University of Technology, Czech Republic

TAS @ UPMARC

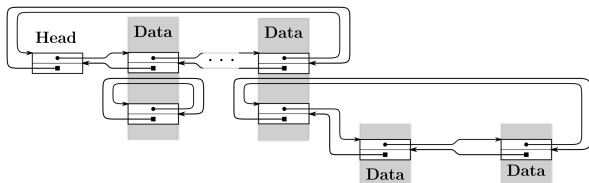
---

<sup>†</sup>Published in *Proc. of CAV'13*

# Shape Analysis

## ■ Shape analysis:

- reasoning about programs with dynamic linked data structures
- notoriously **difficult**: infinite sets of complex graphs

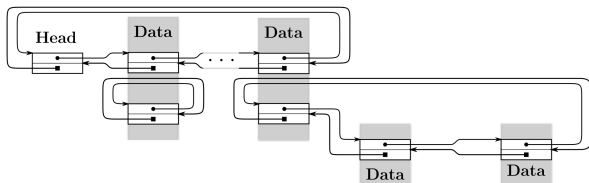


- **memory safety**: invalid dereferences, double free, memory leakage
- **error line reachability** (assertions), **shape invariance** (testers), ...

# Shape Analysis

## ■ Shape analysis:

- reasoning about programs with dynamic linked data structures
- notoriously **difficult**: infinite sets of complex graphs



- **memory safety**: invalid dereferences, double free, memory leakage
- **error line reachability** (assertions), **shape invariance** (testers), ...

## ■ Existing **solutions**:

- often specialized (lists)
- require human help (loop invariants, inductive predicates)
- low scalability

## ■ Separation Logic

😊 local reasoning: well scalable

☹️ fixed abstraction

## ■ Separation Logic

- 😊 local reasoning: **well scalable**
- ☹️ **fixed abstraction**

## ■ Abstract Regular Tree Model Checking (ARTMC)

- 😊 uses tree automata (TA): **flexible** and **refinable abstraction**
- ☹️ monolithic encoding of the heap: **limited scalability**

# The Forest Automata-based Approach

- Introduced at CAV'11.

# The Forest Automata-based Approach

- Introduced at CAV'11.
- Combines
  - 😊 flexibility of ARTMC

# The Forest Automata-based Approach

- Introduced at CAV'11.
- Combines
  - 😊 flexibility of ARTMCwith
  - 😊 scalability of SL



# The Forest Automata-based Approach

- Introduced at CAV'11.
- Combines
  - ☺ flexibility of ARTMCwith
  - ☺ scalability of SLby
  - splitting heaps into tree components

# The Forest Automata-based Approach

- Introduced at CAV'11.

- Combines

☺ flexibility of ARTMC

with

☺ scalability of SL

by

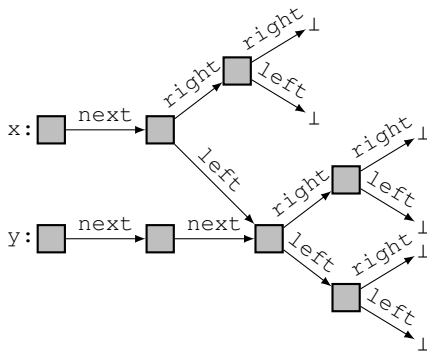
- splitting heaps into tree components

and

- using tree automata to represent sets of tree components of heaps

# Heap Representation

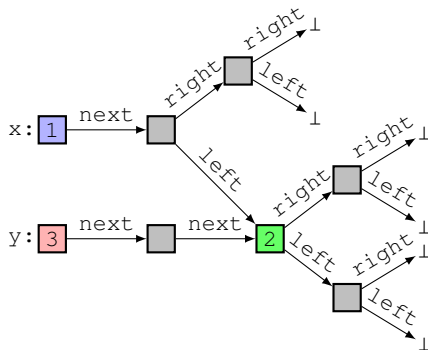
## ■ Forest decomposition of a heap



# Heap Representation

- Forest decomposition of a heap

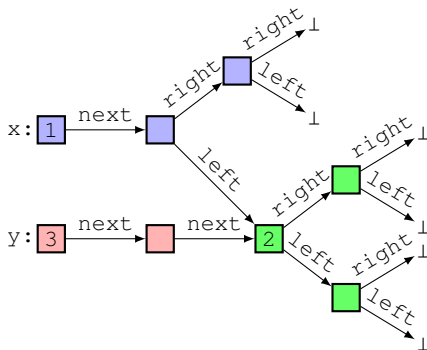
- **Forest decomposition** of a heap
- ▶ Identify **cut-points** ← nodes referenced:
    - by variables, or
    - multiple times



# Heap Representation

## ■ Forest decomposition of a heap

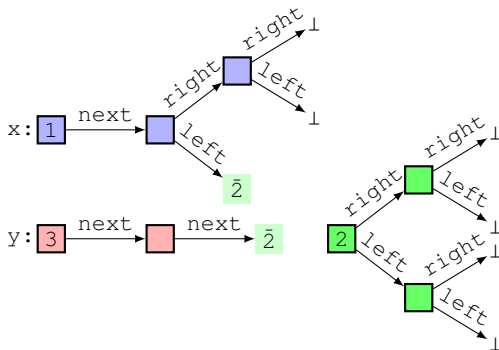
- ▶ Identify **cut-points** ← nodes referenced:
  - by variables, or
  - multiple times
- ▶ Split the heap into **tree components**



# Heap Representation

## ■ Forest decomposition of a heap

- ▶ Identify **cut-points** ← nodes referenced:
  - by variables, or
  - multiple times
- ▶ Split the heap into **tree components**
- ▶ **References** are explicit



# Heap Representation

■ a heap  $h \mapsto$  a forest  $(\uparrow_1, \uparrow_2, \dots, \uparrow_n)$

# Heap Representation

- a **heap**  $h \mapsto$  a **forest**  $(\blacktriangleright_1, \blacktriangleright_2, \dots, \blacktriangleright_n)$
- a **set of heaps**  $\mathcal{H} \mapsto \{(\blacktriangleright_1, \blacktriangleright_2, \dots, \blacktriangleright_n), (\blacktriangleright'_1, \blacktriangleright'_2, \dots, \blacktriangleright'_m), \dots\}$



# Heap Representation

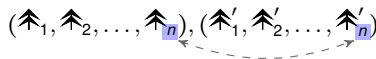
- a **heap**  $h \mapsto$  a **forest**  $(\blacktriangleright_1, \blacktriangleright_2, \dots, \blacktriangleright_n)$
- a **set of heaps**  $\mathcal{H} \mapsto \{(\blacktriangleright_1, \blacktriangleright_2, \dots, \blacktriangleright_n), (\blacktriangleright'_1, \blacktriangleright'_2, \dots, \blacktriangleright'_m), \dots\}$ 
  - split  $\mathcal{H}$  into classes of forests with:

- 1 the same number of trees  $(\blacktriangleright_1, \blacktriangleright_2, \dots, \blacktriangleright_n), (\blacktriangleright'_1, \blacktriangleright'_2, \dots, \blacktriangleright'_n)$

# Heap Representation

- a **heap**  $h \mapsto$  a **forest**  $(\blacktriangleright_1, \blacktriangleright_2, \dots, \blacktriangleright_n)$
- a **set of heaps**  $\mathcal{H} \mapsto \{(\blacktriangleright_1, \blacktriangleright_2, \dots, \blacktriangleright_n), (\blacktriangleright'_1, \blacktriangleright'_2, \dots, \blacktriangleright'_m), \dots\}$ 
  - split  $\mathcal{H}$  into classes of forests with:

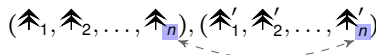
- 1 the same number of trees
- 2 having the same references



# Heap Representation

- a **heap**  $h \mapsto$  a **forest**  $(\blacktriangleright_1, \blacktriangleright_2, \dots, \blacktriangleright_n)$
- a **set of heaps**  $\mathcal{H} \mapsto \{(\blacktriangleright_1, \blacktriangleright_2, \dots, \blacktriangleright_n), (\blacktriangleright'_1, \blacktriangleright'_2, \dots, \blacktriangleright'_m), \dots\}$ 
  - split  $\mathcal{H}$  into classes of forests with:

- 1 the same number of trees
- 2 having the same references
- 3 in the same order

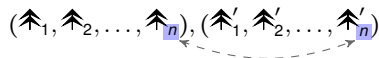


# Heap Representation

- a **heap**  $h \mapsto$  a **forest**  $(\blacktriangleright_1, \blacktriangleright_2, \dots, \blacktriangleright_n)$
- a **set of heaps**  $\mathcal{H} \mapsto \{(\blacktriangleright_1, \blacktriangleright_2, \dots, \blacktriangleright_n), (\blacktriangleright'_1, \blacktriangleright'_2, \dots, \blacktriangleright'_m), \dots\}$

▸ split  $\mathcal{H}$  into classes of forests with:

- 1 the same number of trees
- 2 having the same references
- 3 in the same order



▸ i.e., with the same **interconnection** of **tree components**

# Heap Representation

■ a **heap**  $h \mapsto$  a **forest**  $(\blacktriangleright_1, \blacktriangleright_2, \dots, \blacktriangleright_n)$

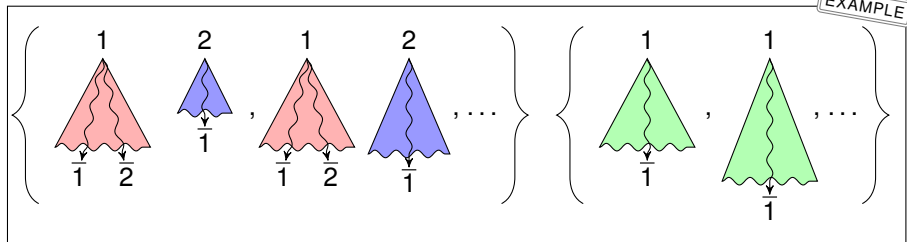
■ a **set of heaps**  $\mathcal{H} \mapsto \{(\blacktriangleright_1, \blacktriangleright_2, \dots, \blacktriangleright_n), (\blacktriangleright'_1, \blacktriangleright'_2, \dots, \blacktriangleright'_m), \dots\}$

▸ split  $\mathcal{H}$  into classes of forests with:

- 1 the same number of trees
- 2 having the same references
- 3 in the same order

$(\blacktriangleright_1, \blacktriangleright_2, \dots, \blacktriangleright_n), (\blacktriangleright'_1, \blacktriangleright'_2, \dots, \blacktriangleright'_n)$

▸ i.e., with the same **interconnection** of **tree components**



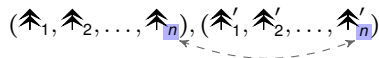
# Heap Representation

■ a **heap**  $h \mapsto$  a **forest**  $(\blacktriangleright_1, \blacktriangleright_2, \dots, \blacktriangleright_n)$

■ a **set of heaps**  $\mathcal{H} \mapsto \{(\blacktriangleright_1, \blacktriangleright_2, \dots, \blacktriangleright_n), (\blacktriangleright'_1, \blacktriangleright'_2, \dots, \blacktriangleright'_m), \dots\}$

▸ split  $\mathcal{H}$  into classes of forests with:

- 1 the same number of trees
- 2 having the same references
- 3 in the same order



▸ i.e., with the same **interconnection** of **tree components**

■ **Cartesian representation** of classes of  $\mathcal{H}$ :

$$\{(\blacktriangleright_1, \blacktriangleright_2, \dots, \blacktriangleright_n), (\blacktriangleright'_1, \blacktriangleright'_2, \dots, \blacktriangleright'_n), \dots\}$$

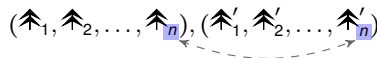
# Heap Representation

■ a **heap**  $h \mapsto$  a **forest**  $(\uparrow_1, \uparrow_2, \dots, \uparrow_n)$

■ a **set of heaps**  $\mathcal{H} \mapsto \{(\uparrow_1, \uparrow_2, \dots, \uparrow_n), (\uparrow'_1, \uparrow'_2, \dots, \uparrow'_m), \dots\}$

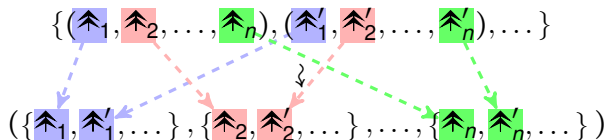
▸ split  $\mathcal{H}$  into classes of forests with:

- 1 the same number of trees
- 2 having the same references
- 3 in the same order



▸ i.e., with the same **interconnection** of **tree components**

■ **Cartesian representation** of classes of  $\mathcal{H}$ :



▸ We assume working with **rectangular classes**, i.e., for a class  $C$ ,  
 $(\uparrow, \uparrow), (\uparrow, \uparrow) \in C \Rightarrow (\uparrow, \uparrow), (\uparrow, \uparrow) \in C$ , or  $C$  is split.

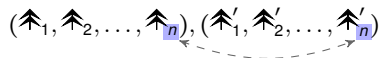
# Heap Representation

■ a **heap**  $h \mapsto$  a **forest**  $(\uparrow_1, \uparrow_2, \dots, \uparrow_n)$

■ a **set of heaps**  $\mathcal{H} \mapsto \{(\uparrow_1, \uparrow_2, \dots, \uparrow_n), (\uparrow'_1, \uparrow'_2, \dots, \uparrow'_m), \dots\}$

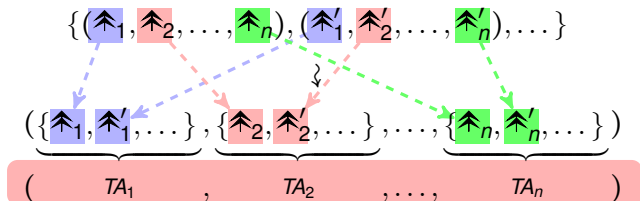
▸ split  $\mathcal{H}$  into classes of forests with:

- 1 the same number of trees
- 2 having the same references
- 3 in the same order



▸ i.e., with the same **interconnection** of **tree components**

■ **Cartesian representation** of classes of  $\mathcal{H}$ :



▸ We assume working with **rectangular classes**, i.e., for a class  $C$ ,  
 $(\uparrow, \uparrow), (\uparrow, \uparrow) \in C \Rightarrow (\uparrow, \uparrow), (\uparrow, \uparrow) \in C$ , or  $C$  is split.



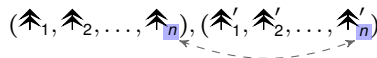
# Heap Representation

■ a **heap**  $h \mapsto$  a **forest**  $(\uparrow_1, \uparrow_2, \dots, \uparrow_n)$

■ a **set of heaps**  $\mathcal{H} \mapsto \{(\uparrow_1, \uparrow_2, \dots, \uparrow_n), (\uparrow'_1, \uparrow'_2, \dots, \uparrow'_m), \dots\}$

▸ split  $\mathcal{H}$  into classes of forests with:

- 1 the same number of trees
- 2 having the same references
- 3 in the same order

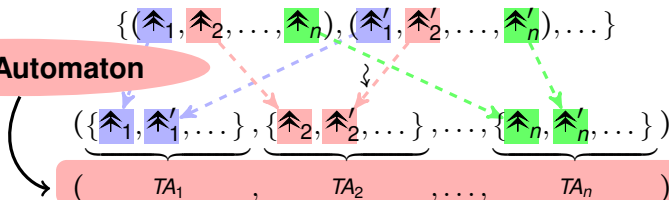


▸ i.e., with the same **interconnection** of **tree components**

■ **Cartesian representation** of classes of  $\mathcal{H}$ :

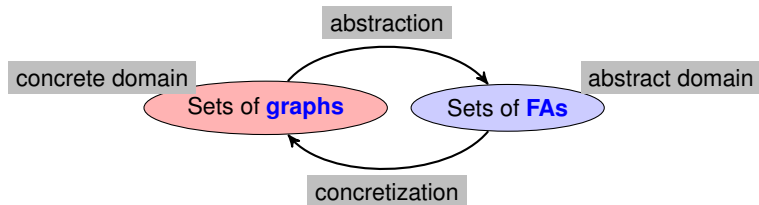
$$\{(\uparrow_1, \uparrow_2, \dots, \uparrow_n), (\uparrow'_1, \uparrow'_2, \dots, \uparrow'_n), \dots\}$$

**Forest Automaton**

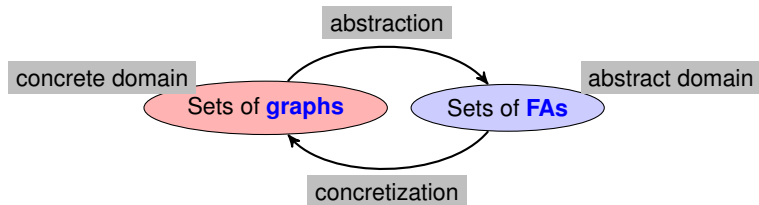


▸ We assume working with **rectangular classes**, i.e., for a class  $C$ ,  
 $(\uparrow, \uparrow), (\uparrow, \uparrow) \in C \Rightarrow (\uparrow, \uparrow), (\uparrow, \uparrow) \in C$ , or  $C$  is split.

# Abstract Interpretation



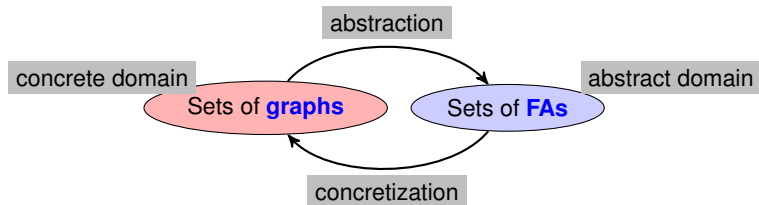
# Abstract Interpretation



## Statements

- `x := new T()`
- `delete(x)`
- `x := null`
- `x := y`
- `x := y.next`
- `x.next := y`
- `if/while (x == y)`

# Abstract Interpretation

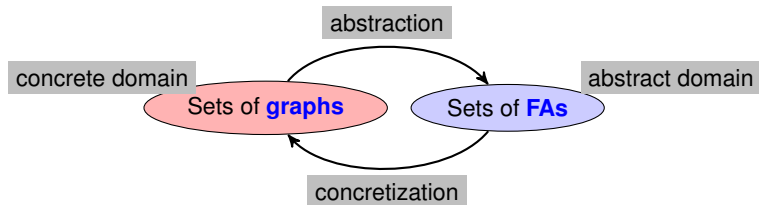


## Statements

- `x := new T()`
- `delete(x)`
- `x := null`
- `x := y`
- `x := y.next`
- `x.next := y`
- `if/while (x == y)`

## Abstract Transformers

# Abstract Interpretation



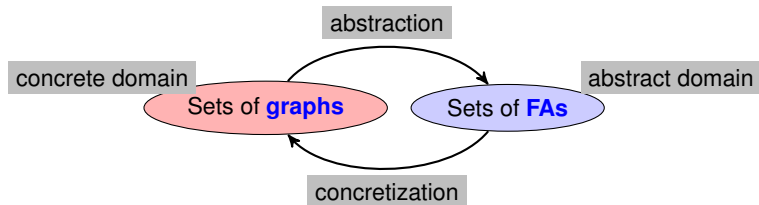
## Statements

- `x := new T()`
- `delete(x)`
- `x := null`
- `x := y`
- `x := y.next`
- `x.next := y`
- `if/while (x == y)`

## Abstract Transformers

append a TA

# Abstract Interpretation



## Statements

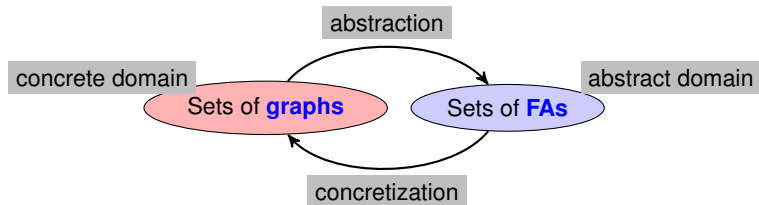
- `x := new T()`
- `delete(x)`
- `x := null`
- `x := y`
- `x := y.next`
- `x.next := y`
- `if/while (x == y)`

## Abstract Transformers

append a TA

remove a TA

# Abstract Interpretation



## Statements

- `x := new T()`
- `delete(x)`
- `x := null`
- `x := y`
- `x := y.next`
- `x.next := y`
- `if/while (x == y)`

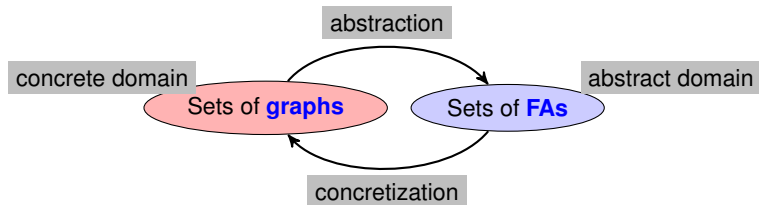
## Abstract Transformers

append a TA

remove a TA

modify transitions

# Abstract Interpretation



## Statements

- `x := new T()`
- `delete(x)`
- `x := null`
- `x := y`
- `x := y.next`
- `x.next := y`
- `if/while (x == y)`

## Abstract Transformers

append a TA

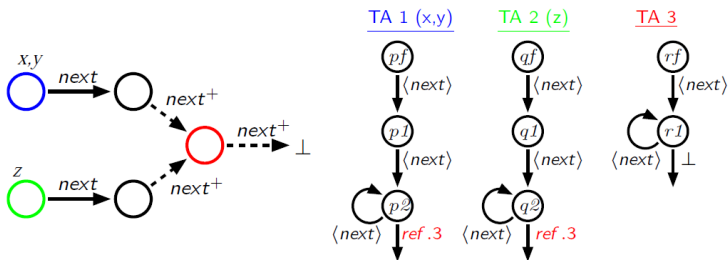
remove a TA

modify transitions

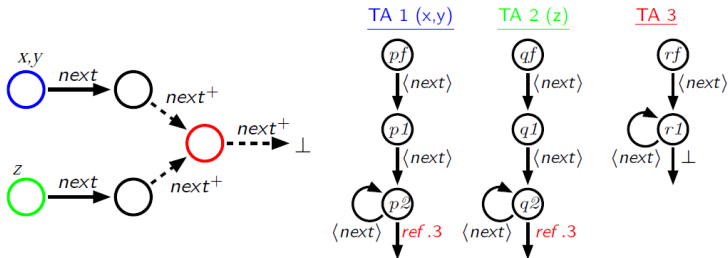
check symbols on transitions



# Abstract Transformers for Pointer Updates

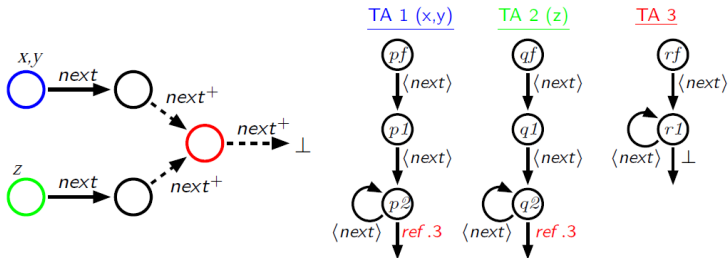


# Abstract Transformers for Pointer Updates

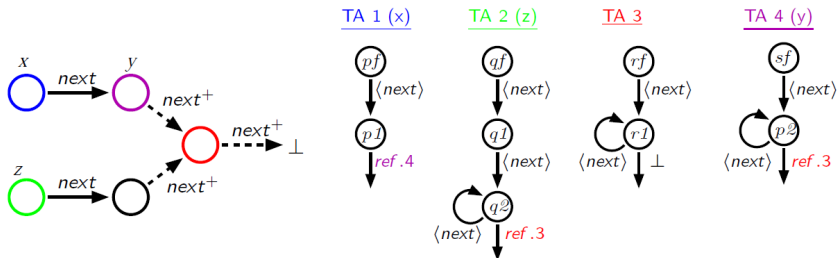


■  $y := x.next$

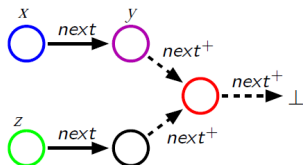
# Abstract Transformers for Pointer Updates



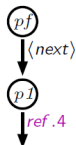
■  $y := x.next$



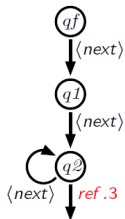
# Abstract Transformers for Pointer Updates



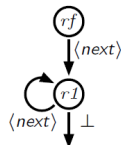
TA 1 ( $x$ )



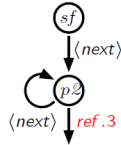
TA 2 ( $z$ )



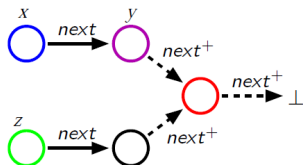
TA 3



TA 4 ( $y$ )

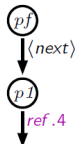


# Abstract Transformers for Pointer Updates

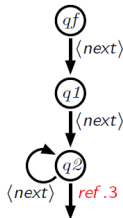


■  $x.next := z;$

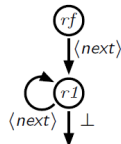
TA 1 ( $x$ )



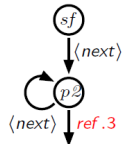
TA 2 ( $z$ )



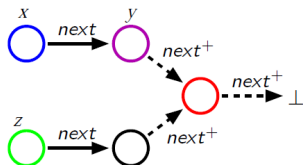
TA 3



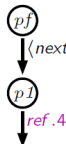
TA 4 ( $y$ )



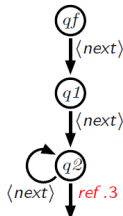
# Abstract Transformers for Pointer Updates



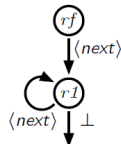
TA 1 (x)



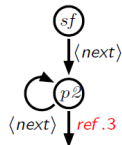
TA 2 (z)



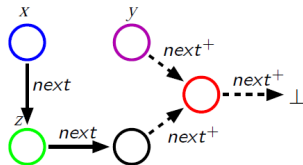
TA 3



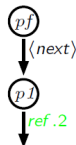
TA 4 (y)



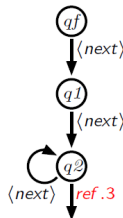
■  $x.next := z;$



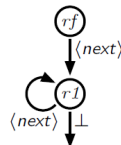
TA 1 (x)



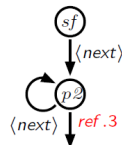
TA 2 (z)



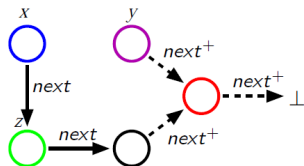
TA 3



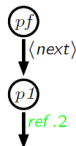
TA 4 (y)



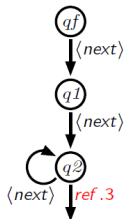
# Abstract Transformers for Pointer Updates



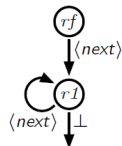
TA 1 ( $x$ )



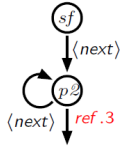
TA 2 ( $z$ )



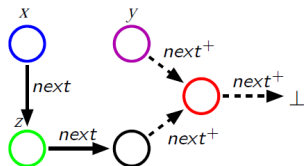
TA 3



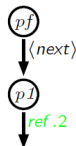
TA 4 ( $y$ )



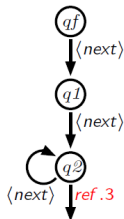
# Abstract Transformers for Pointer Updates



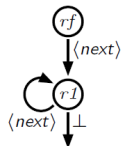
TA 1 ( $x$ )



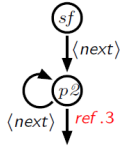
TA 2 ( $z$ )



TA 3



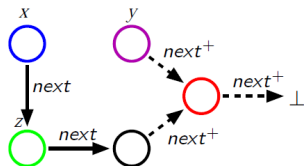
TA 4 ( $y$ )



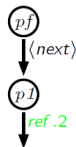
■  $Z := X;$



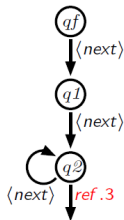
# Abstract Transformers for Pointer Updates



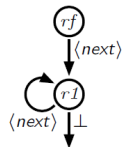
TA 1 ( $x$ )



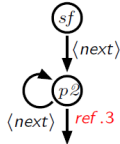
TA 2 ( $z$ )



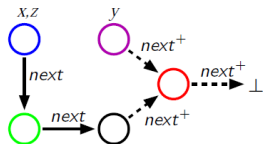
TA 3



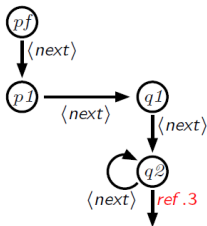
TA 4 ( $y$ )



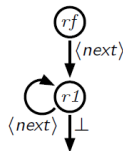
■  $Z := X;$



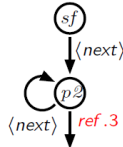
TA 1 ( $x, z$ )



TA 3



TA 4 ( $y$ )

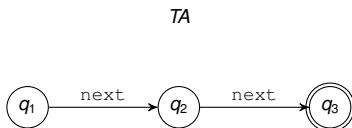


- **Abstraction** on forest automata ( $TA_1, \dots, TA_n$ )

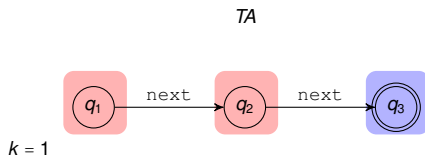
- **Abstraction** on forest automata  $(TA_1, \dots, TA_n)$ 
  - **collapse** states of component TAs  $\leadsto (TA_1^\alpha, \dots, TA_n^\alpha)$

- **Abstraction** on forest automata  $(TA_1, \dots, TA_n)$ 
  - **collapse** states of component TAs  $\rightsquigarrow (TA_1^\alpha, \dots, TA_n^\alpha)$
  - **finite-height** abstraction (from ARTMC)
    - collapse states with languages whose prefixes match **up to height  $k$**

- **Abstraction** on forest automata ( $TA_1, \dots, TA_n$ )
  - **collapse** states of component TAs  $\leadsto (TA_1^\alpha, \dots, TA_n^\alpha)$
  - **finite-height** abstraction (from ARTMC)
    - collapse states with languages whose prefixes match **up to height  $k$**

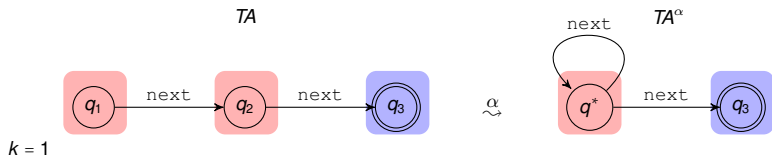


- **Abstraction** on forest automata ( $TA_1, \dots, TA_n$ )
  - **collapse** states of component TAs  $\leadsto (TA_1^\alpha, \dots, TA_n^\alpha)$
  - **finite-height** abstraction (from ARTMC)
    - collapse states with languages whose prefixes match **up to height  $k$**



# Widening

- **Abstraction** on forest automata ( $TA_1, \dots, TA_n$ )
  - **collapse** states of component TAs  $\rightsquigarrow (TA_1^\alpha, \dots, TA_n^\alpha)$
  - **finite-height** abstraction (from ARTMC)
    - collapse states with languages whose prefixes match **up to height  $k$**



# Nondeterministic Tree Automata

- For efficiency reasons, we **never determinize** TAs.
- All operations done on NTAs, including:
  - **inclusion checking**: based on **antichains** and **simulations**,
    - discarding macro-states during an implicit subset construction,
    - inclusion on (normalized) FA can be checked **component-wise** —used for detecting the **fixpoint**
  - **size reduction**: based on **simulation equivalences**.
    - collapsing simulation-equivalent states.



# Summary

The so-far-presented:

# Summary

The so-far-presented:

- 😊 works well for **singly linked lists** (SLLs), **trees**,  
SLLs with **head/tail pointers**, trees with **root pointers**, ...

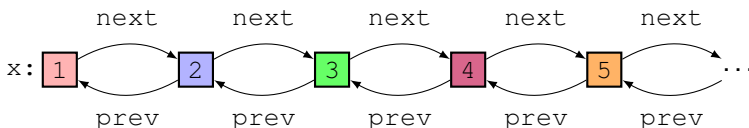
# Summary

$$(\uparrow_1, \uparrow_2, \dots, \uparrow_n) \approx (\uparrow'_1, \uparrow'_2, \dots, \uparrow'_n)$$

...

The so-far-presented:

- 😊 works well for **singly linked lists (SLLs)**, **trees**,  
SLLs with **head/tail pointers**, trees with **root pointers**, ...
- 😞 fails for more complex data structures
  - ▶ **unbounded** number of **cut-points**  $\leadsto \infty$  **classes** of  $\mathcal{H}$



- doubly linked lists (DLLs), circular lists, nested lists,
- trees with parent pointers,
- skip lists

## ■ Hierarchical Forest Automata

- FAs are **symbols** (**boxes**) of FAs of a **higher level**
- a **hierarchy** of FAs

## ■ Hierarchical Forest Automata

- FAs are **symbols** (**boxes**) of FAs of a **higher level**
- a **hierarchy** of FAs
- intuition: replace **repeated subgraphs** by a **single symbol**, **hiding** some cut-points

# Hierarchical Forest Automata

## ■ Hierarchical Forest Automata

- FAs are **symbols** (**boxes**) of FAs of a **higher level**
- a **hierarchy** of FAs
- intuition: replace **repeated subgraphs** by a **single symbol**, **hiding** some cut-points

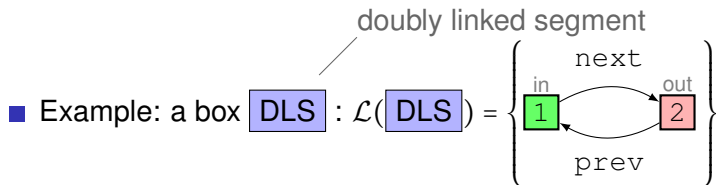
doubly linked segment

■ Example: a box DLS

# Hierarchical Forest Automata

## ■ Hierarchical Forest Automata

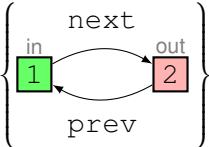
- FAs are **symbols** (**boxes**) of FAs of a **higher level**
- a **hierarchy** of FAs
- intuition: replace **repeated subgraphs** by a **single symbol**, **hiding** some cut-points



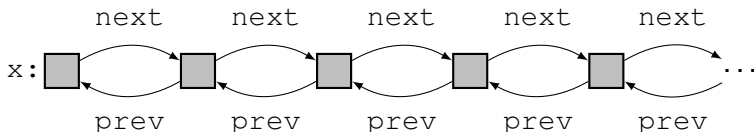
# Hierarchical Forest Automata

## ■ Hierarchical Forest Automata

- FAs are **symbols** (**boxes**) of FAs of a **higher level**
- a **hierarchy** of FAs
- intuition: replace **repeated subgraphs** by a **single symbol**, **hiding** some cut-points

■ Example: a box **DLS** :  $\mathcal{L}(\text{DLS}) =$  

doubly linked segment

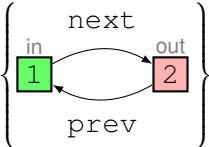




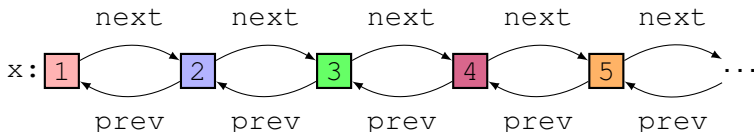
# Hierarchical Forest Automata

## ■ Hierarchical Forest Automata

- FAs are **symbols** (**boxes**) of FAs of a **higher level**
- a **hierarchy** of FAs
- intuition: replace **repeated subgraphs** by a **single symbol**, **hiding** some cut-points

■ Example: a box **DLS** :  $\mathcal{L}(\text{DLS}) =$  

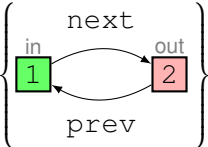
doubly linked segment



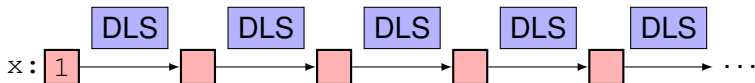
# Hierarchical Forest Automata

## ■ Hierarchical Forest Automata

- FAs are **symbols** (**boxes**) of FAs of a **higher level**
- a **hierarchy** of FAs
- intuition: replace **repeated subgraphs** by a **single symbol**, **hiding** some cut-points

■ Example: a box  $\text{DLS} : \mathcal{L}(\text{DLS}) =$  

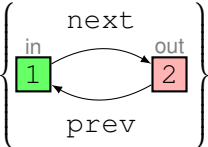
The diagram shows a doubly linked segment (DLS) represented as a box. The label  $\mathcal{L}(\text{DLS})$  is followed by a diagram of the segment. The segment consists of two nodes, 1 and 2, connected by edges labeled 'next' and 'prev'. Node 1 is green and labeled 'in', and node 2 is red and labeled 'out'.



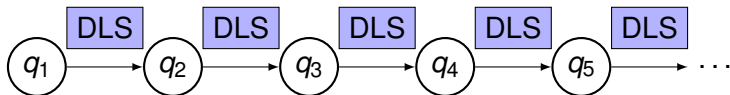
# Hierarchical Forest Automata

## ■ Hierarchical Forest Automata

- FAs are **symbols** (**boxes**) of FAs of a **higher level**
- a **hierarchy** of FAs
- intuition: replace **repeated subgraphs** by a **single symbol**, **hiding** some cut-points

■ Example: a box **DLS** :  $\mathcal{L}(\text{DLS}) =$  

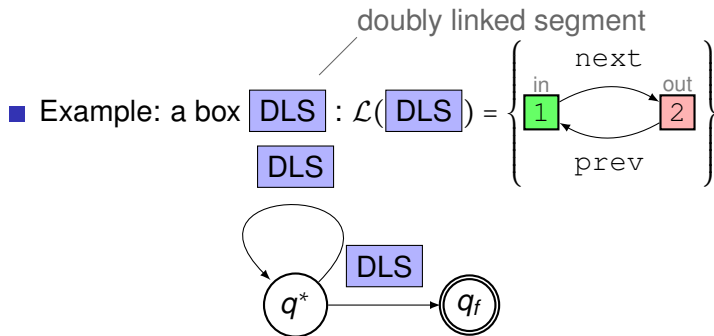
The diagram shows a doubly linked segment (DLS) represented as a box. The label  $\mathcal{L}(\text{DLS})$  is followed by a large curly brace containing a subgraph. This subgraph consists of two nodes: a green node labeled '1' with an 'in' label above it, and a red node labeled '2' with an 'out' label above it. A curved arrow labeled 'next' points from node 1 to node 2, and a curved arrow labeled 'prev' points from node 2 back to node 1. A line points from the text 'doubly linked segment' to the curly brace.



# Hierarchical Forest Automata

## ■ Hierarchical Forest Automata

- FAs are **symbols** (**boxes**) of FAs of a **higher level**
- a **hierarchy** of FAs
- intuition: replace **repeated subgraphs** by a **single symbol**, **hiding** some cut-points



## The Challenge

How to find the “right” boxes?

## The Challenge

How to find the “right” boxes?

- CAV'11 — database of boxes
- CAV'13 — automatic discovery

# Learning of Boxes

- compromise between

# Learning of Boxes

- compromise between
  - **reusability**: use on different heaps of the same kind  
     $\leadsto$  use **small** boxes

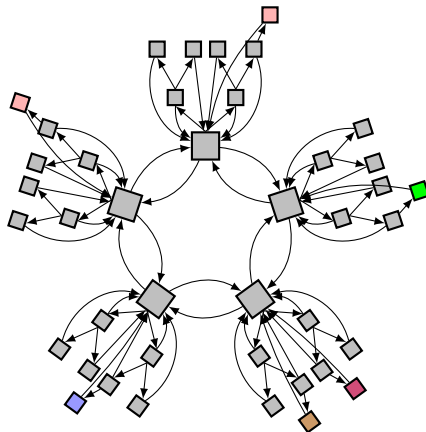


# Learning of Boxes

## ■ compromise between

- **reusability**: use on different heaps of the same kind

~> use **small** boxes

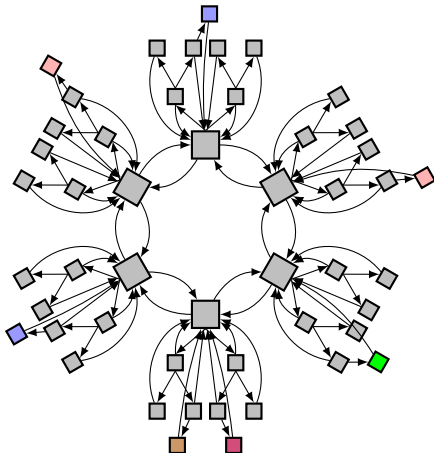


# Learning of Boxes

## ■ compromise between

- **reusability**: use on different heaps of the same kind

~ use **small** boxes

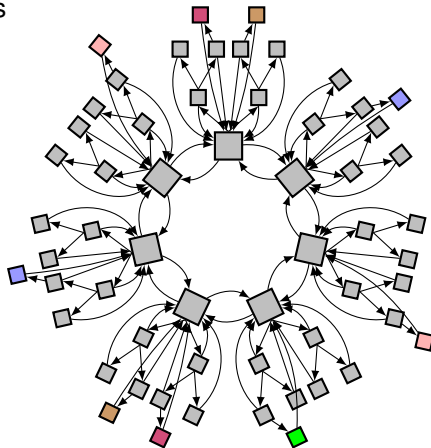


# Learning of Boxes

## ■ compromise between

- **reusability**: use on different heaps of the same kind

↪ use **small** boxes

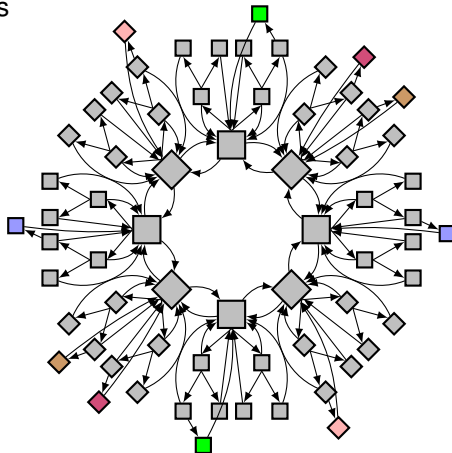


# Learning of Boxes

## ■ compromise between

- **reusability**: use on different heaps of the same kind

↪ use **small** boxes

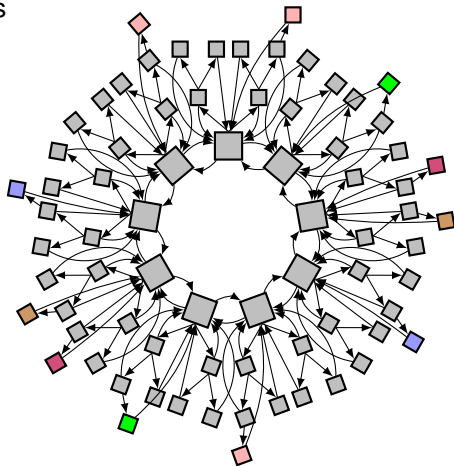


# Learning of Boxes

## ■ compromise between

- **reusability**: use on different heaps of the same kind

~> use **small** boxes



# Learning of Boxes

- compromise between
  - **reusability**: use on different heaps of the same kind  
     $\leadsto$  use **small** boxes

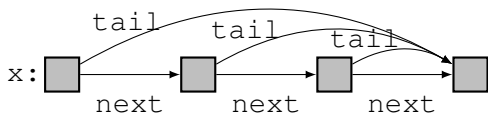
# Learning of Boxes

- compromise between
  - **reusability**: use on different heaps of the same kind
    - ↪ use **small** boxes
  - ability to **hide cut-points**
    - ↪ do not use **too small** boxes

# Learning of Boxes

## ■ compromise between

- **reusability**: use on different heaps of the same kind
  - ↪ use **small** boxes
- ability to **hide cut-points**
  - ↪ do not use **too small** boxes

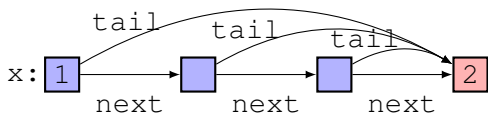




# Learning of Boxes

## ■ compromise between

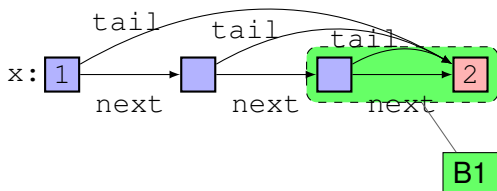
- **reusability**: use on different heaps of the same kind
  - ↪ use **small** boxes
- ability to **hide cut-points**
  - ↪ do not use **too small** boxes



# Learning of Boxes

## ■ compromise between

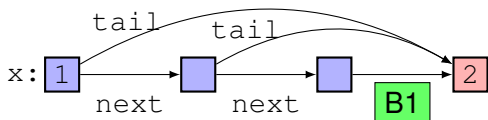
- **reusability**: use on different heaps of the same kind
  - ↪ use **small** boxes
- ability to **hide cut-points**
  - ↪ do not use **too small** boxes



# Learning of Boxes

## ■ compromise between

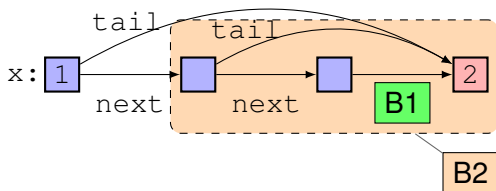
- **reusability**: use on different heaps of the same kind
  - ↪ use **small** boxes
- ability to **hide cut-points**
  - ↪ do not use **too small** boxes



# Learning of Boxes

## ■ compromise between

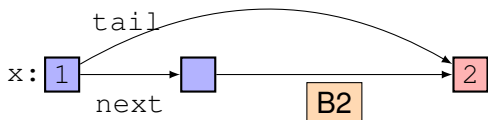
- **reusability**: use on different heaps of the same kind
  - ↪ use **small** boxes
- ability to **hide cut-points**
  - ↪ do not use **too small** boxes



# Learning of Boxes

## ■ compromise between

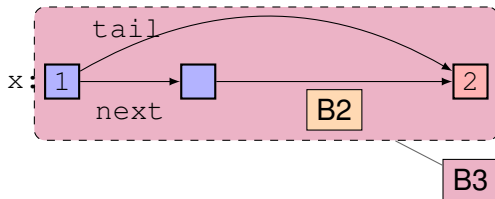
- **reusability**: use on different heaps of the same kind
  - ↪ use **small** boxes
- ability to **hide cut-points**
  - ↪ do not use **too small** boxes



# Learning of Boxes

## ■ compromise between

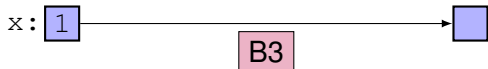
- **reusability**: use on different heaps of the same kind
  - ↪ use **small** boxes
- ability to **hide cut-points**
  - ↪ do not use **too small** boxes



# Learning of Boxes

## ■ compromise between

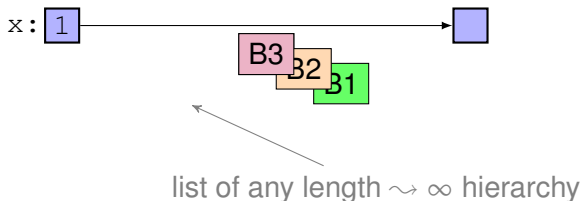
- **reusability**: use on different heaps of the same kind  
     $\leadsto$  use **small** boxes
- ability to **hide cut-points**  
     $\leadsto$  do not use **too small** boxes



# Learning of Boxes

## ■ compromise between

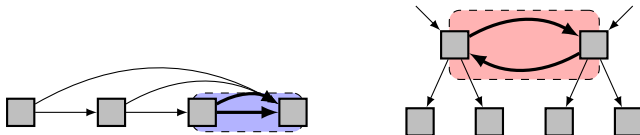
- **reusability**: use on different heaps of the same kind  
     $\leadsto$  use **small** boxes
- ability to **hide cut-points**  
     $\leadsto$  do not use **too small** boxes





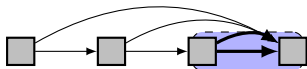
# Learning of Boxes: Knots

## 1 Smallest subgraphs meaningful to be folded:

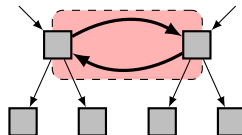


# Learning of Boxes: Knots

- 1 Smallest subgraphs meaningful to be folded:

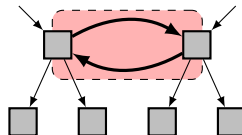
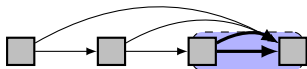


- 2 Handle interface



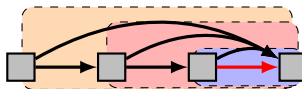
# Learning of Boxes: Knots

- 1 Smallest subgraphs meaningful to be folded:



- 2 Handle interface

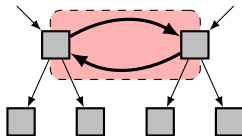
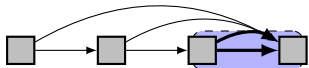
- **compose** intersecting knots



prevent  $\infty$  nesting

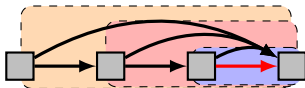
# Learning of Boxes: Knots

- 1 Smallest subgraphs meaningful to be folded:



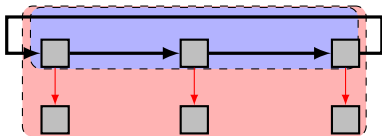
- 2 Handle interface

- **compose** intersecting knots



prevent  $\infty$  nesting

- **enclose** paths from inner nodes to leaves

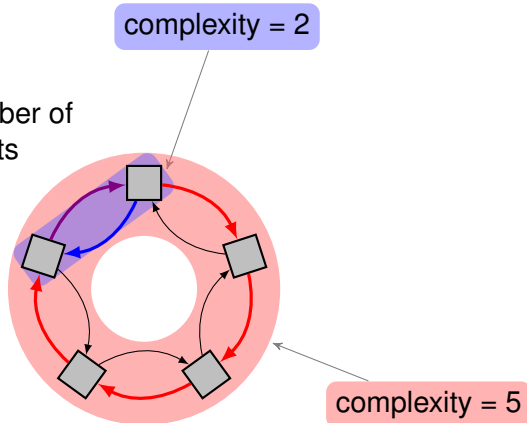


prevent  $\infty$   
interface nodes

- 3 Complexity: max number of cutpoints in basic knots

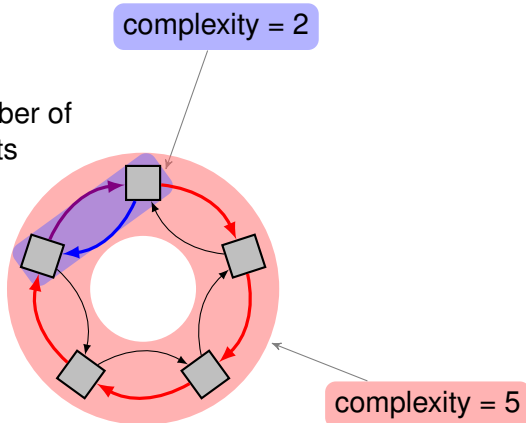
# Learning of Boxes: Knots

- 3 Complexity: max number of cutpoints in basic knots



# Learning of Boxes: Knots

- 3 Complexity: max number of cutpoints in basic knots



- find basic knots with  $1, 2, \dots$  cut-points

# Widening Revisited

- **learning** and **folding** of boxes in the abstraction loop



# Widening Revisited

- learning and folding of boxes in the abstraction loop

## The Goal

Fold boxes that will, after abstraction, appear on cycles of automata.

⇒ hide unboundedly many cut-points

# Widening Revisited

- learning and folding of boxes in the abstraction loop

## The Goal

Fold boxes that will, after abstraction, appear on cycles of automata.

⇒ hide unboundedly many cut-points

1 **Algorithm:** Abstraction Loop

2 *Unfold solo boxes*

3 **repeat**

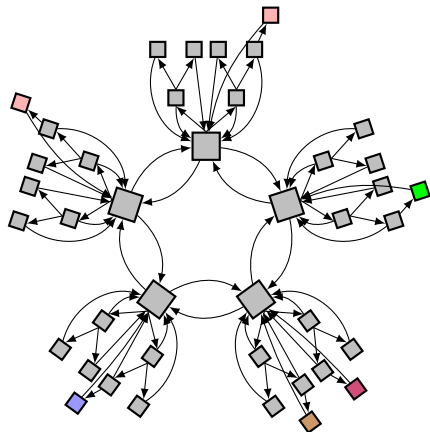
4     *Abstract*

5     *Fold*

6 **until** *fixpoint*

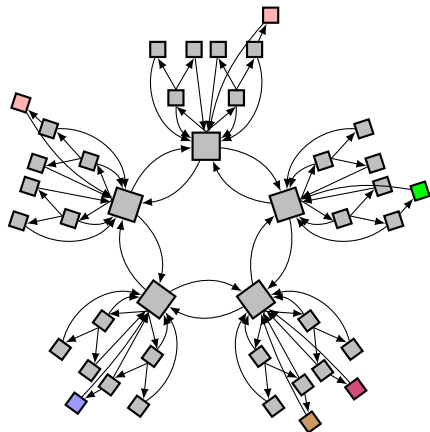
not on a cycle

# Learning of Boxes: Example



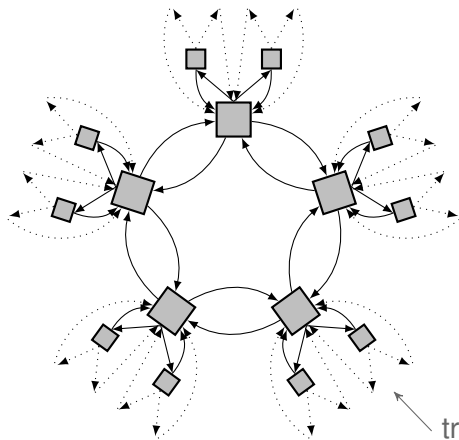
- 1 *Unfold solo boxes*
- 2 **repeat**
- 3     *Abstract*
- 4     *Fold*
- 5 **until** *fixpoint*

# Learning of Boxes: Example



- 1 **Unfold solo boxes**
- 2 **repeat**
- 3     *Abstract*
- 4     *Fold*
- 5 **until fixpoint**

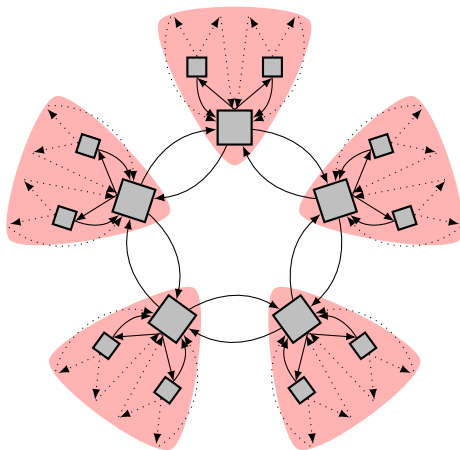
# Learning of Boxes: Example



- 1 *Unfold solo boxes*
- 2 **repeat**
- 3 *Abstract*
- 4 *Fold*
- 5 **until** *fixpoint*

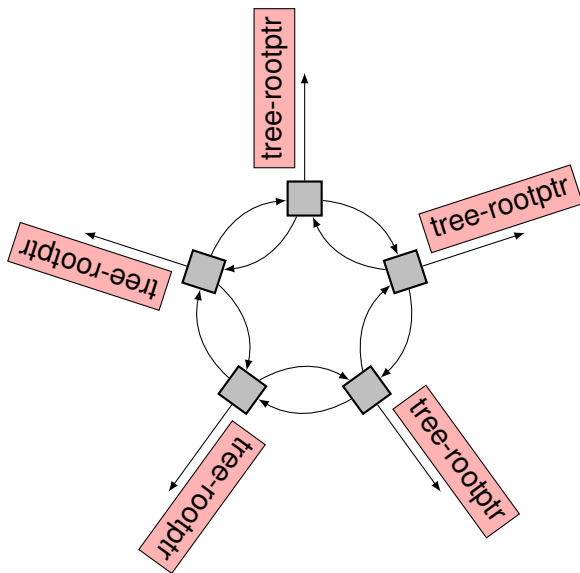
tree with root ptrs of any height

# Learning of Boxes: Example



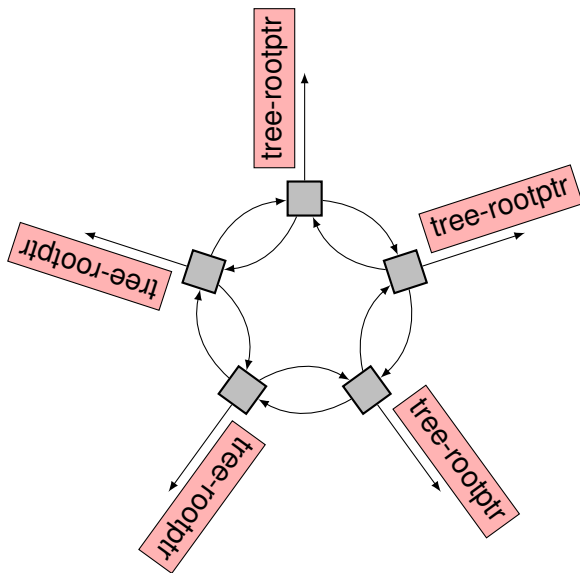
- 1 *Unfold solo boxes*
- 2 **repeat**
- 3     *Abstract*
- 4     *Fold*
- 5 **until** *fixpoint*

# Learning of Boxes: Example



- 1 *Unfold solo boxes*
- 2 **repeat**
- 3     *Abstract*
- 4     *Fold*
- 5 **until** *fixpoint*

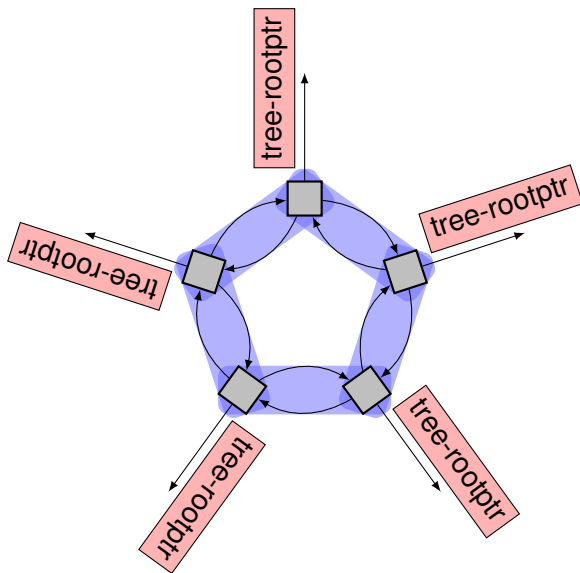
# Learning of Boxes: Example



- 1 *Unfold solo boxes*
- 2 **repeat**
- 3     *Abstract*
- 4     *Fold*
- 5 **until** *fixpoint*

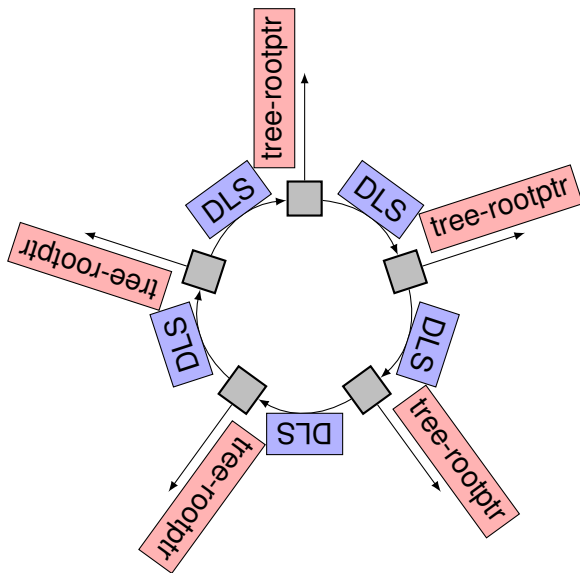


# Learning of Boxes: Example



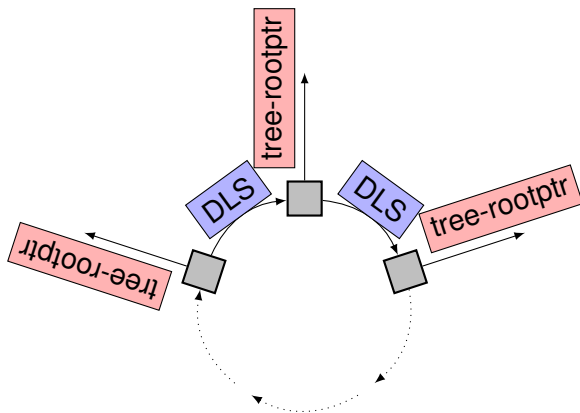
- 1 *Unfold solo boxes*
- 2 **repeat**
- 3     *Abstract*
- 4     *Fold*
- 5 **until** *fixpoint*

# Learning of Boxes: Example



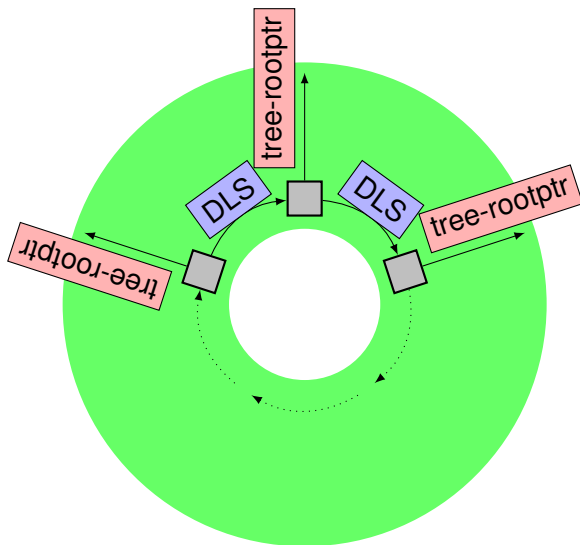
- 1 *Unfold solo boxes*
- 2 **repeat**
- 3     *Abstract*
- 4     *Fold*
- 5 **until** *fixpoint*

# Learning of Boxes: Example



- 1 *Unfold solo boxes*
- 2 **repeat**
- 3     *Abstract*
- 4     *Fold*
- 5 **until** *fixpoint*

# Learning of Boxes: Example



- 1 *Unfold solo boxes*
- 2 **repeat**
- 3     *Abstract*
- 4     *Fold*
- 5 **until** *fixpoint*

# Learning of Boxes: Example

circular-DLL-of  
-trees-rootptr

- 1 *Unfold solo boxes*
- 2 **repeat**
- 3     *Abstract*
- 4     *Fold*
- 5 **until** *fixpoint*

# Experimental Results

- implemented in the **Forester** tool

# Experimental Results

- implemented in the **Forester** tool
- comparison with Predator (a state-of-the-art tool for lists)
  - winner of [HeapManipulation](#) and [MemorySafety](#) of SV-COMP'13

# Experimental Results

- implemented in the **Forester** tool
- comparison with Predator (a state-of-the-art tool for lists)
  - ▶ winner of [HeapManipulation](#) and [MemorySafety](#) of SV-COMP'13

Table: Results of the experiments [s]

Example	FA	Predator	Example	FA	Predator
SLL (delete)	0.04	0.04	DLL (reverse)	0.06	0.03
SLL (bubblesort)	0.04	0.03	DLL (insert)	0.07	0.05
SLL (mergesort)	0.15	0.10	DLL (insertsort <sub>1</sub> )	0.40	0.11
SLL (insertsort)	0.05	0.04	DLL (insertsort <sub>2</sub> )	0.12	0.05
SLL (reverse)	0.03	0.03	DLL of CDLLs	1.25	0.22
SLL+head	0.05	0.03	DLL+subdata	0.09	T
SLL of 0/1 SLLs	0.03	0.11	CDLL	0.03	0.03
SLL <sub>Linux</sub>	0.03	0.03	tree	0.14	Err
SLL of CSLLs	0.73	0.12	tree+parents	0.21	T
SLL of 2CDLLs <sub>Linux</sub>	0.17	0.25	tree+stack	0.08	Err
skip list <sub>2</sub>	0.42	T	tree (DSW) <sup>Deutsch-Schorr-Waite</sup>	0.40	Err
skip list <sub>3</sub>	9.14	T	tree of CSLLs	0.42	Err

timeout

false positive



# Conclusion

Shape analysis with **forest automata**:

- fully **automated**
- very **flexible** framework
- **Forester** tool
- successfully verified:
  - (singly/doubly linked (circular)) **lists** (of (...) lists)
  - **trees**
  - **skip lists**
- not covered here:
  - support for **pointer arithmetic**
  - tracking **ordering** relations
    - P. Abdulla, L. Holík, B. Jonsson, O. Lengál, C.Q. Tring, and T. Vojnar. **Verification of Heap Manipulating Programs with Ordered Data by Extended Forest Automata**. In *Proc. of ATVA'13*.

# Future work

- CEGAR loop
  - **red-black** trees, ...
- **concurrent** data structures
  - lockless skip lists, ...
- **recursive** boxes
  - B+ trees, ...